Mental Math Solutions

	Answer	Solution
1	113	What is seventy-seven plus thirty-six?
2	32	 A composite number is a number with at least one factor in addition to one and the number itself. What is the smallest composite number greater than thirty? 31 is prime, 32 is divisible by 1, 32, and several other numbers
3	45 [mph]	A train travels at an average speed of thirty miles per hour. A car travels at an average speed that is one and a half times as fast as the train. How many miles per hour is the car's average speed? 30*1.5=45
4	[A + B =] 37	When rolling two standard dice the probability of rolling two ones as a reduced common fraction is A over B. What is the value of A plus B? 1/6*1/6 = 1/36, so $1 + 36 = 37$
5	2 [inches]	A rectangle is four inches wide and fifteen inches long. What is the number of inches in the radius of the largest circle that can completely fit inside the rectangle without going outside the rectangle? The shorter dimension of 4 inches limits the diameter of the circle to 4 inches, so the radius would be 2 inches.
6	144	What is one hundred multiplied by one point two and then multiplied by one point two again? 100*1.2 = 120 120*1.2 = 144

7	[A + B =] 5	Abe, Ben, Cara, and Dina are randomly arranged in a line. The probability that Dina stands at the front of the line as a reduced common fraction is A over B. What is the value of A plus B? There are 4! ways to arrange the four people and 3! ways that Dina could be at the front, so the probability is 3!/4! = 1/4, so 1 + 4 = 5
8	5 [rectangles]	How many distinct rectangles with whole number side lengths are possible if the perimeter is twenty inches and a one by nine rectangle counts as the same as a nine by one rectangle? Possible values for (L, W) include (1, 9), (2, 8), (3, 7), (4, 6), (5, 5)

"Math is Cool" Championships -- 2020-21 $\frac{7^{\text{th}}/8^{\text{th}} \text{ Grade}}{7^{\text{th}}}$

Individual Test Solutions

	Answer	Solution
1	100	What is 80 + 90 – 70?
		80 + 90 - 70 = 100
2	[A + B =] 11	The probability that a number chosen randomly from the set $\{1, 2, 3, 4, 5, 6, 7\}$ is odd as a reduced common fraction is A/B. What is the value of A + B?
		4 out of the 7 numbers are odd, so 4/7 is the probability 4 + 7 = 11
3	90 [degrees]	What is the number of degrees in a right angle?
		90 degrees in a right angle
4	40 [nickels]	How many nickels are equal in value to 2 dollars?
		200/5 = 40
5	540	What is the product of 60 and 9? $60 \times 9 = 540$
6	200 [pages]	Rashida has read 30 pages of <i>The Full Cupboard of Life</i> , from the Number One Ladies Detective Agency book series, which is 15 percent of the number of pages in the book. How many pages are in <i>The Full Cupboard of Life</i> ?
7	88	Olaf divides his favorite number by 8 and then adds 3. The result is 14. What is Olaf's favorite number? x/8 + 3 = 14, so $x/8 = 11$, so $x = 88$
8	8 [vertices]	How many vertices (corners) are there on a cube?
9	12	What is the square root of 144? $\sqrt{144} = 12$
10	5	What is the remainder when 77 is divided by 12? 77/12 = 6 r5

11	[x =] 14	Solve the equation for x:
		10x – 25 = 115
		10x - 25 = 115, so 10x = 140, so x = 14
12	6 [days]	A vine grows 6 inches per day. In how many days will the vine be 3
14		feet longer than it is now?
		3 ft = 36 in, 36/6 = 6
12	[A + B =] 9	A jar contains 32 red marbles, 24 green marbles, and 8 blue
10		marbles. The ratio of the total marbles in the jar that are blue is
		A/B, as a reduced common fraction. What is the value of A + B?
		8/64 = 1/8
	221 [:2]	$1+\delta=9$
14		What is the number of square inches in the area of the restangle?
		13 * 17 = 221
	[A + B =] 106	As a decimal, the mean (average) of the four smallest three-digit
15		whole numbers is A.B. where A is a three-digit number and B is a
		single digit. What is the value of $A + B$?
		100 + 101 + 102 + 103 = 406, 406/4 = 101.5, and 101 + 5 = 106
16	30 [bananas]	One cantaloupe costs the same as five oranges. One orange costs
10		the same as three bananas. How many bananas cost the same as
		two cantaloupes?
		1C = 50, 1O = 3B, 1C = 15B, 2C = 30B
17	5 [miles]	A car is driving at an average rate of 30 miles per hour. How many
1.		miles does the car travel in 10 minutes?
	210	10 min is 1/6 of an nour, so 1/6 of $30 = 5$
18	216	
		$\{2, 5, 4, 5, 0, 7, 8, 9, 10\}$
		the first set by 4. What is the sum of all the numbers in the new
		cot2
		2 + 3 + 4 + 5 + 6 + 7 + 8 + 9 + 10 = 54
		4 * 54 = 216
10	6 [elbow	In a doubles tennis match there are two two-person teams. After
17	bumpsl	a certain match, each player gives every other player in the match
		an elbow bump. How many total elbow bumps are exchanged?
		n(n - 1)/2
		4(3)/2 = 6

20	854917632	Garfield writes the words representing the numbers 1 through 9
20		in alphabetical order. Then he replaces each word with the
		number it represents to form a 9-digit number. What is this 9-digit
		number?
		eight, five, four, nine, one, seven, six, three, two becomes 854917632
21	75 [inches]	The perimeter of a parallelogram is 200 inches, and the length of
		the longer side is three times the length of the shorter side. What
		is the number of inches in the length of the longer side?
		L = 3W and 2W + 2L = 200. Substituting 3W for L results in 8W = 200, so W = 25
		and L = 75
າາ	20 [routes]	On the lower half of a hill there are four paths to choose from. All
		four paths lead to the same spot half-way up the hill. From this
		spot to the top there are five paths to choose from. How many
		total routes are there to hike up the hill from bottom to ton?
		4 * 5 = 20
າາ	1 [multiple]	How many positive two-digit multiples of 7 are also multiples of
23		10?
		{14, 21, 28, 35, 42, 49, 56, 70, 77, 84, 91, 98} ∩ {10, 20, 30, 40, 50, 60, 70, 80,
		90} = {70}
21	81	A palindrome is a number that reads the same forwards as
Z4	[palindromes]	backwards, like 232. How many positive three-digit palindromes
		are there in which the three digits are not all the same?
		In each group, 100 – 199, 200 – 299, , 900 - 999, there are 10, for example,
		from 100 – 199 the palindromes are 101, 111, 121, 131, 141, 151, 161, 171,
		181, 191. However, one in each group has all three digits the same, in the case
		of 100 – 199, it is 111. So, there are 9 groups and 9 in each, so 9 * 9 = 81.
25	[A + B =] 59	There are 13 green skittles and 11 red skittles in a jar. Two skittles
23		are taken from the jar at random without replacement. The
		probability as a reduced common fraction that both skittles are
		green is A/B. What is the value of A + B?
		P(G,G) = 13/24 * 12/23 = 13/46
		13 + 46 = 59
26	1270	Let S_1 be the infinite arithmetic series whose first three terms are
20		10, 19, 28, , let S_2 be the infinite geometric series whose first
		three terms are 5, 15, 45, , and let S_3 be the sum of S_1 and S_2 .
		This means that the 1^{st} term of S ₃ equals the sum of the 1^{st} terms
		of S ₁ and S ₂ , the 2 nd term of S ₃ equals the sum of the 2 nd terms of
		S_1 and S_2 , and so on. What is the 6 th term in S_3 ?
		The first 6 terms of S ₁ are: 10, 19. 28. 37. 46. 55
		The first 6 terms of S ₂ are: 5, 15, 45, 135, 405, 1215
		55 + 1215 = 1270

27	16 [times]	Circle B has a radius that is four times the radius of Circle A. How
21		many times larger is the area of Circle B than the area of Circle A?
		The area of Circle A is πr^2 and the area of Circle B is $\pi (4r)^2$, which simplifies to
		$16\pi r^2$, which is 16 times as much area.
20	5	The given system of equations has exactly one solution, (x, y). For
20		this solution what is x + y?
		2x - 3y = 40
		5x + 6y = 19
		$2x - 3y = 40 \rightarrow 4x - 6y = 80 \rightarrow 9x = 99 \rightarrow x = 11$
		5x + 6y = 19 $5x + 6y = 19$
		$22 - 3y = 40 \rightarrow -3y = 18 \rightarrow y = -6 \rightarrow 11 + -6 = 5$
20	[A + B =] 36	In a survey of 600 households, exactly 17% of the households
29		have at least one dog and at least one cat as pets, exactly 12%
		have at least one cat and no dogs as pets, and exactly 27% have at
		least one dog and no cats as pets. The remaining households have
		neither dogs nor cats as pets. The probability, as a reduced
		common fraction, that a household chosen at random from the
		600 households has at least one dog as a pet is A/B. What is the
		value of A + B?
		17% have at least 1 dog and at least 1 cat and 27% have at least 1 dog and no
		cats, so 44% have at least one dog = 44/100 = 11/25
-		11 + 25 = 36
30	11 [matches]	Susan and Lisa are playing a series of tennis matches against
		lesses. The small eval around the 0 is moveable and when Susan
		using a match, she mayor it one number to the right When Lise
		wins a match, she moves is one number to the left. If Susan wins
		three matches and there have been no ties how many total
		matches will they have played when the oval is moved to the
		left-hand 5 for the first time?
		5 4 3 2 1 0 1 2 3 4 5
		The order of who wins each match does not matter in solving this problem. So
		if you assume Lisa wins the first 3 matches, then Susan will win the next 8 so
		that the oval ends up on the left-hand 5. $3 + 8 = 11$

31	[A + B =] 33	Junior has one gallon of red paint and one gallon of blue paint. He takes one cup of red paint and adds it to the gallon of blue paint. After mixing it thoroughly, he takes out one cup of the mixed paint. Inside this cup, the ratio of paint that is blue is A/B, as a
		reduced common fraction. What is the value of A + B? After 1 cup of red paint is added to the blue paint, 16/17 of the mixture is blue paint and 1/17 of the mixture is red paint. Any amount of this mixture that is taken out will have this same ratio, which will be 1/17th red and 16/17 blue,
32	14 [numbers]	and 16 + 17 = 33 In the Venn diagram shown, how many positive whole numbers less than 45 are inside the rectangle but outside both ovals? Positive whole numbers less than 45 Composite numbers Positive whole numbers less than 45 1,2,3,7,11,13,17,19,23, 29,31,37,41,43 S Multiples of 5 Multiples of 5 Multipl
33	35 [inches]	A trapezoid has a height to area ratio of 1:18. The height of the trapezoid is less than 10 inches and both bases have integer lengths. What is the number of inches in the longest possible base of the trapezoid? Reminder: the bases of a trapezoid are the two parallel edges.
		You can get two equations here, Area = $(a + b)h/2$ and Area = $18h \rightarrow 18h = (a + b)h/2 \rightarrow a + b = 36$ Since both are integers and must be positive, one of them is 1 and the other is 35.
34	[A =] 722 _[8]	The base-9 number 567 ₉ equals the base-10 number N. The base- 8 number A ₈ also equals N. What is the value of A? N equals 466. The largest multiple of 8 ² that is less than 466 is 7 * 8 ² , or 448. Then 466 – 448 = 18. The largest multiple of 8 ¹ that is less than 18 is 2 * 8 ¹ , or 16. Then 18 – 16 = 2, which equals 2 * 8 ⁰ . So, 466 = 7 * 8 ² + 2 * 8 ¹ + 2 * 8 ⁰ and the base-8 number is 722 ₈ , so A = 722

35	30 [mph]	Bettina drives at an average rate of 40 miles per hour during the 4-mile drive from home to work in the morning. On the way back from work to home along the same route, she averages 24 miles per hour. What is her overall average rate in miles per hour for the two trips combined? 40 miles in 60 min means she goes 4 miles in 6 min on the way to work 24 miles in 60 min means she goes 4 miles in 10 min on the way home 8 miles in 16 min for the combined trips means 32 miles in 64 min 32(15/16) miles in 64(15/16) min equals 30 miles in 60 min
36	8 [series]	A certain infinite series of numbers is in the form abcabcabc where a, b, and c, each represent a distinct positive single digit number. For example, the series 123123123 matches the given description, whereas 445445445 does not. How many infinite series that match this description exist in which any three adjacent digits add up to more than 21? Note, the series 123123123 and 231231231 count as the same series, since they are infinite series and it therefore cannot be said what digit each series begins or ends with. 589589589
37	[T – S =] 360	An increasing arithmetic sequence begins with 10 as its first term, has 9 more terms, and the common difference is d. If d = 2, then the sum of the 10 terms is S. If d = 10, then the sum of the 10 terms is T. What is the value of T – S? If d = 2 then term number ten equals $10 + 9(2) = 28$, and the sum of the ten numbers, S, would be $(10 + 28)*10/2 = 38*5$ If d = 10 then term number ten equals $10 + 9(10) = 100$, and the sum of the ten numbers, T, would be $(10 + 100)*10/2 = 110*5$ T – S = $110x5 - 38x5 = 550 - 190 = 360$

38	0	Consider the equation $0 = x^2 + kx - 24$. What is the sum of all possible values of k for which the equation has two integer solutions for x? $x-1)(x+24) \rightarrow k = 23$ $(x-2)(x+12) \rightarrow k = 10$ $(x-3)(x+8) \rightarrow k = 5$ $(x-4)(x+6) \rightarrow k = 2$ $(x-6)(x+4) \rightarrow k = -2$ $(x-6)(x+4) \rightarrow k = -2$ $(x-8)(x+3) \rightarrow k = -5$ $(x-12)(x+2) \rightarrow k = -10$ $(x-24)(x+1) \rightarrow k = -23$ $23 + 10 + 5 + 2 + -2 + -5 + -10 + -23 = 0$
39	38 [values]	A data set has six distinct positive integers. The median is 23 and the mean is less than the median. How many possible values of the largest integer in the set are there? If the mean is less than the median, then the sum of the integers in the set must be less than 6 * 23 = 138. The smallest sum possible for the set is 100 when the six integers are 1, 2, 22, 24, 25, 26. Every sum between 100 and 137 is possible, since the set can have the same smallest 5 integers while the largest integer can increase by 1 until the overall sum reaches 137. So, the sums from 100 to 137 are all possible, which means there are 38 possible values for the largest number.
40	[\$] 2000 [dollars]	A local club plans to spend \$10,000 to cover the costs of hosting a baseball game. They expect to sell tickets that will generate a total of \$15,000 in income. If it rains on the day of the game, they won't sell any tickets and the club will lose all the money invested. The weather forecast for the day of game is a 20% probability of rain. On average and in dollars, how much profit can the club expect to earn? 80% of the time they will earn \$5000 and 20% of the time they will lose \$10000. .8(5000) + .2(-10000) = 4000 - 2000 = 2000

Multiple Choice Solutions

	Answer	Solution	
USE THE	JSE THE FOLLOWING INFORMATION TO SOLVE PROBLEMS #1 THROUGH #4.		
The equation $y = 6x - 10$ has an infinite number of solutions in the form (x, y) where x stands for one number and y stands for the resulting number when the number that x represents is multiplied by 6 and then 10 is subtracted. For example (2, 2) is a solution, because if x is replaced with two, the resulting value of y is 6(2) - 10, which equals 2.			
1	C	Which of the ordered pairs is also a solution to the equation? A) (-1, 4) B) (-1, -4) C) (3, 8) D) (3, 14) E) (4, 16) 6(3) - 10 = 8, so (3, 8) is a solution	
2	D	When x equals 100, what does y equal? A) 50/3 B) 30 C) 300 D) 590 E) 610 y = 6(100) - 10 = 590	
3	В	What is the value of x in the ordered pair (x, 20)? A) 1. $\overline{6}$ B) 5 C) 15 D) 18 E) 110 20 = 6x - 10, 30 = 6x, x = 5	



E	В	Which competitive eating record has the largest number of
3		kilograms ingested?
		A) Baked Beans B) Rice Balls C) Waffles
		D) Gelatin
		E) Watanmalan
		C) water meion
		Rice Balls has the tallest pink bar.
6	E	Each food record in the table can be ranked based on how it compares to the other foods' rate of consumption and weight ingested. For example, we would rank Butter as 15 th (last) for total weight ingested, and 14 th for rate of ingestion. With rankings, the lower the number the better the ranking. In other words, a rank of 1 is better than a rank of 10.
		What is the lowest sum when the rank of rate of ingestion is added to the rank of total weight ingested, for any of the 15 foods listed? A) 35 B) 18 C) 7 D) 6 E) 5 Waffles has rank 3 for rate of ingestion and rank 2 for total
		weight ingested, so $3 + 2 = 5$.
7	B	The ranks for rate of ingestion go from best to worst as you read from left to right on the bar graph. If the graph were to be redrawn so that the ranks for total weight ingested were to go from best to worst as you read left to right, how many records would not move from their current spot on the graph? A) 0 B) 1 C) 2 D) 4 E) 7
		The only one that would not move is the 'Peas' category, which is in the 8 th position for rate of ingestion, and is also in the 8 th position for total weight ingested.

USE THE FOLLOWING INFORMATION TO SOLVE PROBLEMS #8 THROUGH #10.			
Consider the segment shown with length 9 cm as Shape 0.			
	Shap	9 cm	
Imagine th to form th	ne middle three cer ne new shape shown	ntimeters were removed and replaced with two 3-cm segments n , which is Shape 1.	
	Shap	be 1	
Then the p replaced b	process is repeated by two segments of	l where all four of the segments have their middle third the same length to create Shape 2.	
•	, 	\wedge	
Shape 2			
8	С	What is the sum of the lengths of the four segments in Shape 1? A) 9 cm	
		B) 10 cm	
		C) 12 cm	
		D) 27 cm	
		4 segments that are 3 cm each has a total length of 12 cm	
9	D	A figure made of three Shape 2s is shown here.	
		What is the sum of the lengths of all the segments in the perimeter of this figure?	
		A) 36 cm	
		B) 42 cm	
		D) 48 cm	
		E) 54 cm	
		Each Shape 2 has sixteen 1-cm long segments, so 3 * 16 = 48 cm.	



Team Test Solutions

	Answer	Solution
1	53	Evaluate the expression: $11(2 + 5) - 24$ 11(2 + 5) - 24 = 11(7) - 24 = 77 - 24 = 53
2	6 [colors]	All the socks in a drawer are mixed up and there is at least one pair of each color. If socks are pulled randomly from the drawer, the minimum number needed to be pulled in order to get at least one matching pair is 7 socks. How many different sock colors are in the drawer?
		match. When you draw the 7 th one, there must be a match.
3	50 [%]	A chessboard is a square grid with 8 rows and 8 columns of small squares. When a game is set up pieces are placed on all squares in two rows on one side of the board and on all squares in two rows on the other side of the board. At the start of the game, what percent of the squares on the board have pieces on them? There are a total of $8*8 = 64$ squares on the board and there are 8 squares in each row. Since four rows have pieces on all their squares, then there are $4*8 = 32$ pieces. $32/64 = 1/2$ or 50% .
4	2	 While Romy is out walking, she takes three 90 degree right turns and ends up facing north. What direction was she facing before the three turns? Answer 1 for North, 2 for East, 3 for South, and 4 for West. When going east, turning 90 degrees right results in going south. When going south, turning 90 degrees right results in going west. When going west, turning 90 degrees right results in going north. So she was going east when she started.
5	[A + B =] 8	The product of $\frac{1}{3} \cdot \frac{3}{5} \cdot \frac{5}{7}$ as a reduced common fraction is A/B. What is the value of A + B? 1/3*3/5*/5/7 = 1/7, so 1 + 7 = 8

6	149 [degrees]	Three of the angles in a certain quadrilateral are 100 degrees, 82 degrees, and 67 degrees. What is the number of degrees in the sum of the measures of the smallest two angles in the quadrilateral? 100 + 82 + 67 = 249, 360 – 249 = 111, so 111 is the fourth angle and the two smallest angles are 67 and 82, so 67 + 82 = 149
7	90 [cm]	In a regular polygon all sides have the same length. In the series of regular pentagons shown here, going left to right each successive pentagon has side lengths that are three-fifths the length of the sides of the previous pentagon. If the lengths of the sides on the largest pentagon are 50 cm, then what is the number of centimeters in the perimeter of the smallest pentagon? $\int_{50 \text{ cm}} \int_{50 \text{ cm}$
8	2 [inches]	A basketball team of 5 players has an average height of 74 inches. A new player joins the team who is 7 ft 2 in tall. Reminder: there are 12 inches in 1 foot. By how many inches does the average height of the team increase when the new player joins? 5 * 74 = 370 7 ft 2 in = 86 in 370 + 86 = 456 456/6 = 76 76 - 74 = 2

9	[A + B =] 156	A rectangular prism is 3 inches by 6 inches by 8 inches and has a cylindrical hole in it as shown. The diameter of the cylinder is 4 inches. The volume of this solid is A – B π cubic inches, where A is a positive three-digit integer and B is a positive two-digit integer. What is the value of A + B? What is the value of A + B? 3 in 3 in The volume of the prism is 8*6*3 = 144 The volume of the cylinder is $2^2\pi^*3 = 12\pi$ The volume of the solid is 144 - 12π so A = 144 and B = 12 and A + B = 156
10	[A + B =] 38	Aaron and Bonita are playing a game. Each chooses two numbers randomly from the list {1,2,3} and multiplies them together. Individual numbers can be chosen multiple times. For example, it's possible for Aaron to choose two 1s and for Bonita to also choose two 1s. A person only wins if they have the bigger product. As a reduced common fraction, the probability that Bonita wins is A/B. What is the value of A + B? The list of possible outcomes for each person is: $(1,1)=1, (1,2)=2,$ (1,3)=3, (2,1)=2, (2,2)=4, (2,3)=6, (3,1)=3, (3,2)=6, (3,3)=9 There are 9*9 = 81 total outcomes in which one person's outcome is compared to the other person's outcome. Each of these 81 outcomes is equally likely. Winning outcomes for Bonita include: 9v6 - 2 outcomes, 9v4 - 1 outcome, 9v3 - 2 outcomes, 9v2 - 2 outcomes, 9v1 - 1 outcome, 6v4 - 2 outcomes, 6v3 - 4 outcomes, 6v2 - 4 outcomes, 6v1 - 2 outcomes, 4v3 - 2 outcomes, 4v2 - 2 outcomes, 4v1 - 1 outcome, 3v2 - 4 outcomes, $3v1 - 2$ outcomes, $2v1 - 2$ outcomes So, $2 + 1 + 2 + 2 + 1 + 2 + 4 + 4 + 2 + 2 + 2 + 1 + 4 + 2 + 2 = 33$ and the probability is $33/81 = 11/27$ and $11 + 27 = 38$

Linda Moore Triple Jump Solutions

	Answer	Solution
1	[A + B =] 38	In the sentence, 'The quick brown fox jumps over the lazy dog', the ratio of e's to total letters as a reduced common fraction is A/B. What is the value of A + B? There are 35 total letters and 3 e's, so the ratio is 3/35 and 3 + 35 = 38
2	25	If x = 10 and y = -5, then what is the value of the expression? $x^{2} + 2xy + y^{2}$ $10^{2} + 2(10)(-5) + (-5)^{2} = 100 - 100 + 25 = 25$
3	36 [minutes]	Thomas the Tank Engine travels at an average rate of 10 miles per hour. How many minutes does it take him to travel 6 miles? 6/10*60 = 36
4	[\$] 20 [dollars]	The currency system in the USA has \$1 bills, \$2 bills, \$5 bills, \$10 bills, \$20 bills, \$50 bills, and some other bills worth more than \$50. Malik has 5 bills in his wallet worth 51 dollars. What is the number of dollars in the value of the largest bill? \$51 dollars with 5 bills is possible in two ways: 1) if there is one \$1 bill, three \$10 bills, and one \$20 bill or 2) if there is one \$1 bill, two \$5 bills, and two \$20 bills. In either case the largest bill is the \$20 bill.

5	[A + B =] 7	The slope of the line shown as a reduced common fraction is A/B. What is the value of A + B?
		(64)/(22) = 10/4 = 5/2, so $5 + 2 = 7$
6	[E + F =] 29	In the expression A/B + C/D, each letter is replaced with a distinct digit from the set {3,4,6,7}. The smallest possible value that can result from this process is the reduced common fraction E/F. What is the value of E + F? Check $3/7 + 4/6$ and $3/6 + 4/7$. The first one is $46/42$ and the second one is $45/42$, so $45/42$ is smaller and it simplifies to $15/14$, so $15 + 14 = 29$
7	6 [mixtures]	A jar has a total of 7 beads in it. The beads are all either red or blue, and there is at least one of each color. How many different sets of 7 beads are possible that match this description? For example, one set would be 1 red and 6 blue. $(R, B) \rightarrow (1, 6), (2, 5), (3, 4), (4, 3), (5, 2), (6, 1)$



10	34 [rectangles]	How mai angles a	ny recta re right	ngles of angles.	any size	e are in	the draw	ring? Assume all
		2-flat ho 6-vertica 6-taller 4-1.5 x a 3-double 2-double 2-double 2-double 2-2.5 x a 2-triple 1-overal 1-rectan one	prizontal al stubb horizon is wide t e tall ho e wide tal do is wide tal wide tal ll rectan igle mac	l ones y ones tal ones taller ho rizontal aller hor uble wic taller horiz gle le of two	rizontal ones rizontal de horizo rizontal zontal on o vertica	ones ones ontal on ones nes l stubby	es y ones and	d one flat horizontal

College Bowl Round #1 Solutions

	Answer	Solution
1	4 [weeks]	Selina plays soccer three days a week for two hours each day. How many weeks will it take her to play twenty-four hours of soccer? 6 hours per week 24/6 = 4
2	44	What is the product of twenty-four, one sixth, and eleven? 24*1/6*11 = 44
3	115 [bad guys]	Jack Frost can freeze three bad guys in two minutes. Elsa can freeze seven bad guys in three minutes. Working together, how many bad guys could they freeze in thirty minutes? 3 guys in 2 min = 9 guys in 6 min 7 guys in 3 min = 14 guys in 6 min 9 + 14 = 23, 23 *5 = 115
4	80 [inches]	What is the number of inches in the perimeter of a right triangle with legs of length sixteen and thirty inches? (8, 15, 17) is a Pythagorean triple, so (16, 30, 34) is too. 16 + 30 + 34 = 80
5	92	Austin's scores for three math tests are eighty-nine, ninety-seven, and ninety. What score would he need on his fourth test to have an average of ninety-two? 89 + 97 + 90 + x = 4(92) 276 + x = 368, x = 92

6	135 [minutes]	An airplane cruises at an average rate of five hundred miles per hour. A bullet train travels at an average rate of two hundred miles per hour. How many minutes longer does a bullet train take to make the same seven-hundred-and-fifty-mile trip? 750/500 = 1.5 hrs = 90 min 750/200 = 3.75 hrs = 225 min 225 - 90 = 135
7	28 [in ²]	A square has side lengths of six inches. If the sides are all increased by thirty-three and one third percent, what is the number of square inches in the positive difference between the area of the new square and the area of the original square? 6*1.333333333333333333333333333333333333
8	37 [rounds]	A group of kids are playing a certain card game where six cards are played every round. How many rounds will it take them to play two hundred and twenty-two cards? 222/6 = 37
9	127 [cents]	Riley has three quarters, two dimes, and thirty-two pennies. What is the total number of cents in Riley's money? 3(.25) + 2(.10) + .32 = 1.27 = 127 cents
10	8 [hours]	How many hours would it take Nat to drive two hundred and thirty-two miles if she drives at an average rate of twenty-nine miles per hour? 232/29 = 8

"Math is Cool" Championships -- 2020-21 High School

College Bowl Round #2 Solutions

	Answer	Solution
1	114 [cents]	Together, a water bottle and a bag of chips cost two dollars and thirty-eight cents. In cents, how much does the bag of chips cost if it is ten cents cheaper than the water? 238 = w + w - 10 2w = 248, $w = 124$, $c = 114$ cents
2	399	What is the product of twenty-one and nineteen? 21*19 = 399
3	81	What is the positive difference between forty squared and forty- one squared? $41^2 - 40^2 = (41 + 40)(41 - 40) = 81*1 = 81$
4	196 [inches]	An equilateral triangle has a perimeter of one hundred and forty- seven inches. What is the perimeter, in inches, of a square with the same side length as the triangle? 147/3 = 49 49*4 = 196
5	4 [factors]	What is the number of distinct prime factors in thirty thousand three hundred? 30300 = 300*101 + 3*2 ² *5 ² *101, So 2, 3, 5, and 101
6	96 [ways]	How many ways can the letters A-B-C-D-E be put in order, not counting any arrangements that begin with E? 5! - 4! = 120 - 24 = 96

7	47	The first two Fibonacci numbers are one and one. What is the sum of the seventh and ninth Fibonacci numbers? 1, 1, 2, 3, 5, 8, 13, 21, 34 13 + 34 = 47
8	18 [inches]	What is the number of inches in the radius of a circle with a circumference of thirty-six pi inches? d = 36, r = 18
9	62	 What is the next term in the sequence that begins two, six, fourteen, thirty, and so on? 2, 6, 14, 30, is increasing by powers of 2, +4, +8, +16,, so 30 + 32 = 62 will be the next number
10	[A + B =] 115	Two cards are randomly drawn from a standard deck without replacement. As a reduced common fraction, the probability that the first card is a diamond and the second card is black is A over B, where A is a two-digit whole number and B is a three-digit whole number. What is the value of A plus B? 1/4*26/51 = 13/102, so $13 + 102 = 115$

"Math is Cool" Championships -- 2020-21 High School

College Bowl Round #3 Solutions

	Answer	Solution
1	394	What is the sum of thirteen squared and fifteen squared? $13^2 + 15^2 = 169 + 225 = 394$
2	23	What is fifty percent of ten percent of four hundred and sixty? .5*.1*460 = .5*46 = 23
3	10 [shots]	Miriam makes seventy-five percent of her free throws. If she shoots forty free throws, how many shots will she miss? .25*40 = 10
4	64	Find the product of the mean, median, and mode of the following set of data: two, four, one, three, four, six, and eight 2, 4, 1, 3, 4, 6, 8 1 + 2 + 3 + 4 + 4 + 6 + 8 = 28, 28/7 = 4 Median, Median and Mode = 4 $4^3 = 64$
5	24 [cups]	How many cups are in one and a half gallons? 4 C = 1 Q, 4 Q = 1 G, 16 C = 1 G, 24 C = 1.5 G
6	40,320	What is the product of all the numbers from one to eight inclusive? 8! = 40320
7	[A + B =] 157	Jeff plays Tetris for twenty-five minutes on all twenty-nine days during the month of February in a leap year. The number of hours Jeff plays Tetris in February is the reduced common fraction A over B. What is the value of A plus B? 25/60*29 = 5/12*29 = 145/12, so $145 + 12 = 157$

8	33 [days]	Thanos is trying to find six stones to complete his collection. If it takes him five and a half days on average to find each stone, how many total days will he need to find all six stones? 5.5 * 6 = 33
9	7	Rita thinks of a number in her head, then adds seventy to the number, then divides the outcome by eleven. Her final number is seven what number did Rita start with? (x + 70)/11 = 7, x + 70 = 77, x = 7
10	2,431	What is the product of the prime numbers between ten and eighteen? 11*13*17 = 2431